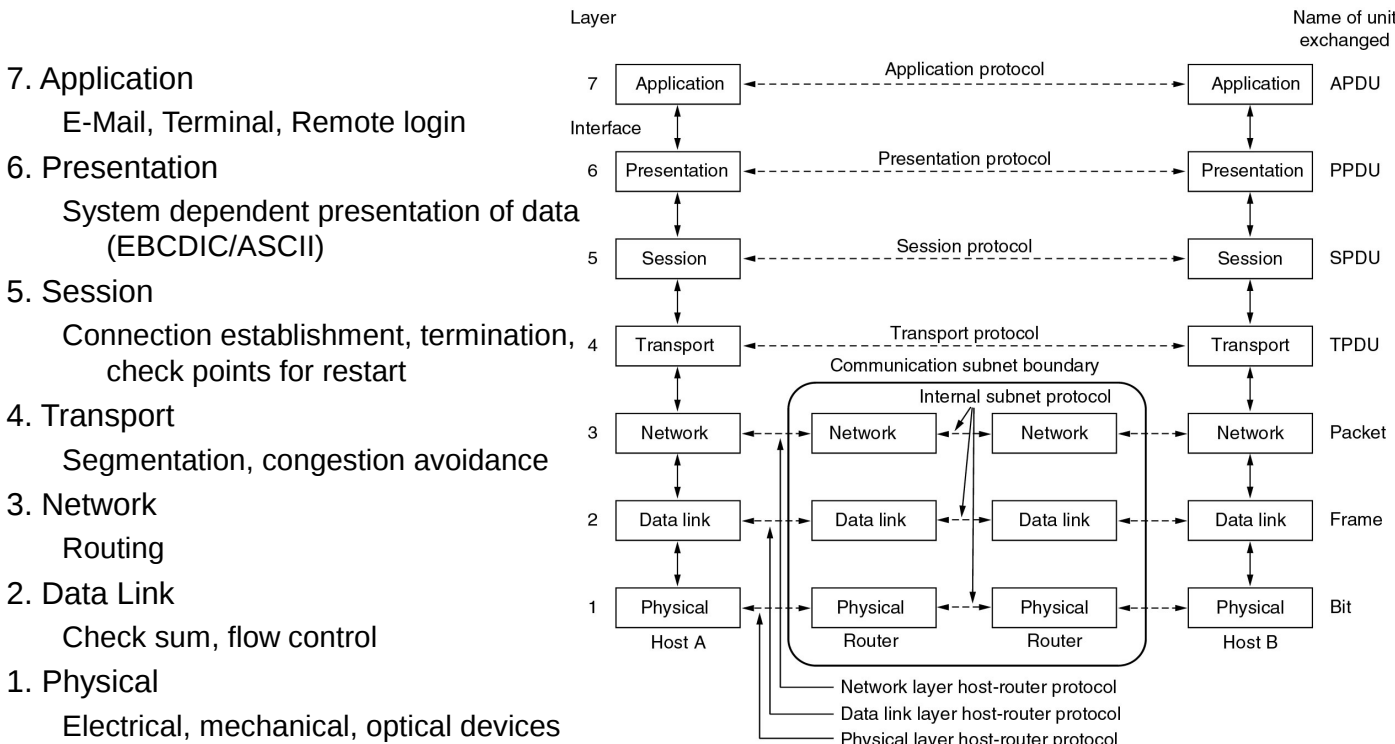


Data Link Layer

ISO/OSI Reference Model

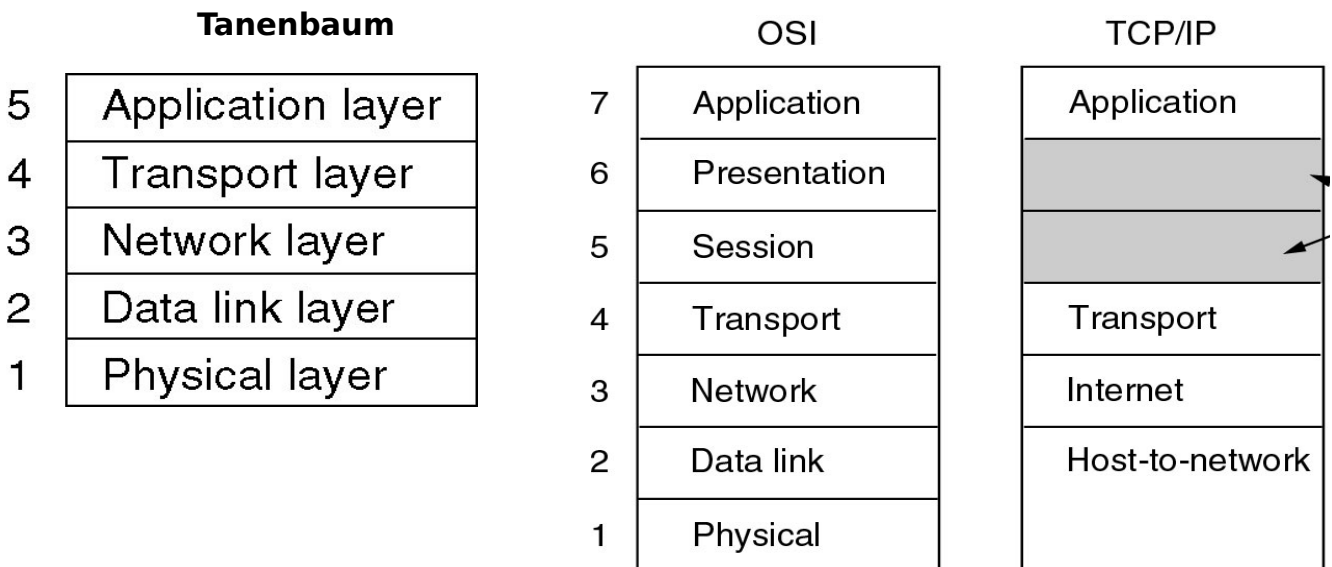


Layers of the Internet - TCP/IP Layers

Application	Telnet, FTP, HTTP, SMTP (E-Mail), DNS, ...
Transport	TCP (Transmission Control Protocol) UDP (User Datagram Protocol)
Network	IP (Internet Protocol) + ICMP (Internet Control Message Protocol) + IGMP (Internet Group Management Protocol)
Host-to-network	LAN (z.B. Ethernet, Token Ring etc.)

Hybride Model

We use Tanenbaum's hybride model



(Tanenbaum)

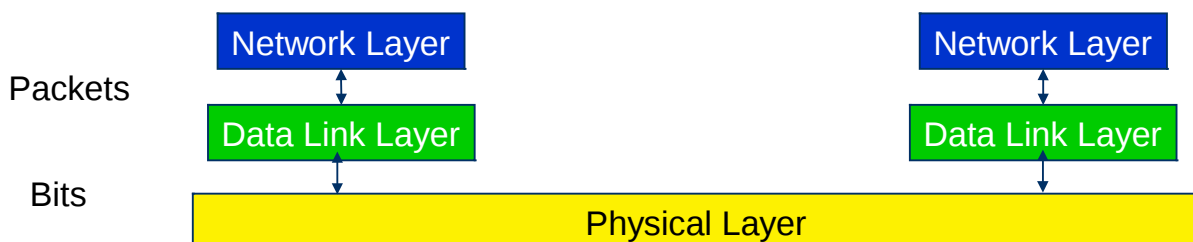
Data Link Layer

- Tasks of the data link layer:
 - Providing services for the network layer
 - Frames
 - Error control
 - Flow control
- Error detection and correction
 - Error correcting codes

Medium Access Control

Services of the Data Link Layer

- The situation of the data link layer
 - the physical layer transmits bits
 - without structure, possibly with errors
- The network layer requires following from the data link layer:
 - transmission without errors
 - transmission of structured data
 - data packets or data stream
 - reliable data flow

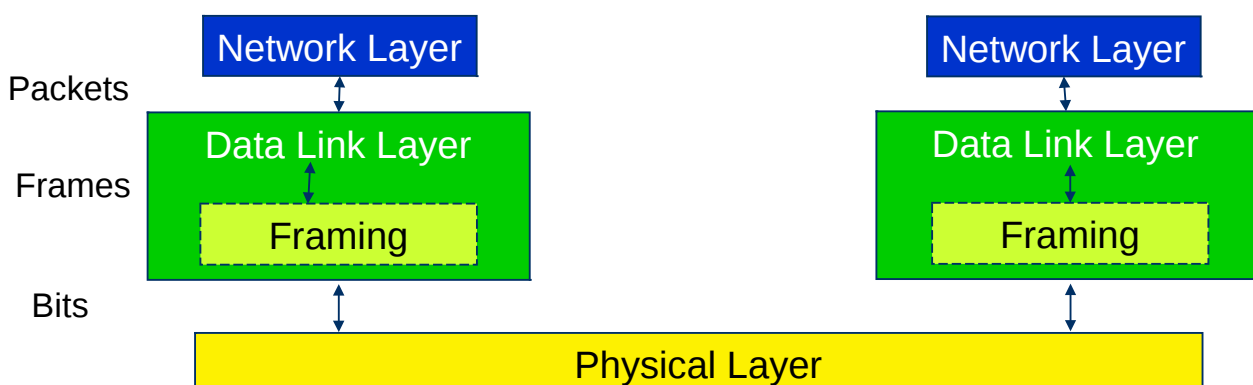


Distinction: Service and Implementation

- Example
 - The network layer requires a connectionless reliable service
 - The data link layer **internally** implements a connection oriented service with error control
- Other combinations are also possible

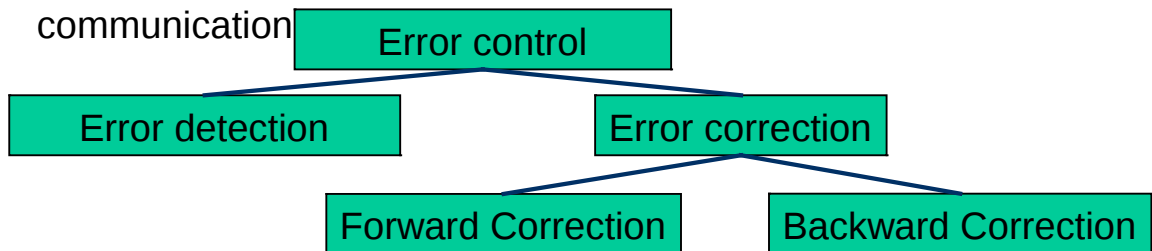
Frames

- Divide the bit stream of the physical layer into peaces: into **frames**
 - Necessary for error control
 - The frames are the packets of the data link layer
- Fragmentation (and defragmentation at the receiver) is necessary, if the packets of the network layer are larger that the frames



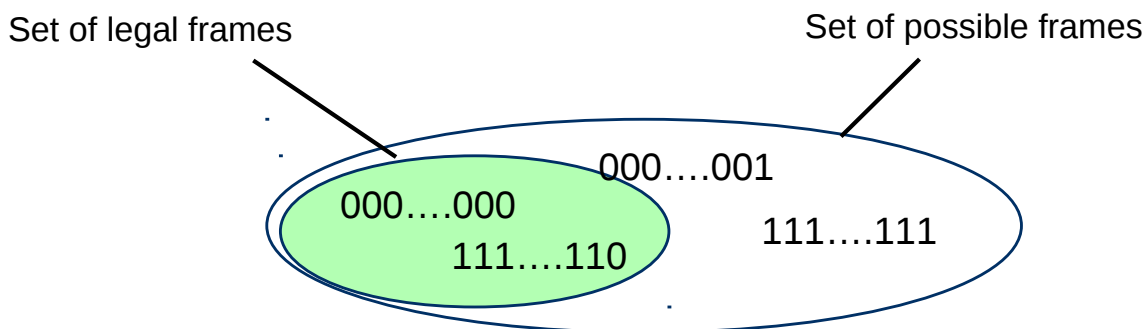
Error Control

- The minimum service required from the data link layer
 - by using frames
- Error detection: detects if there are incorrectly transmitted bits
- Error correction: Cleaning bit errors
 - Forward Error Correction
 - Using redundant code, which allows to correct the error without retransmission
 - Backward Error Correction
 - After detecting an error, the error will be corrected using additional communication



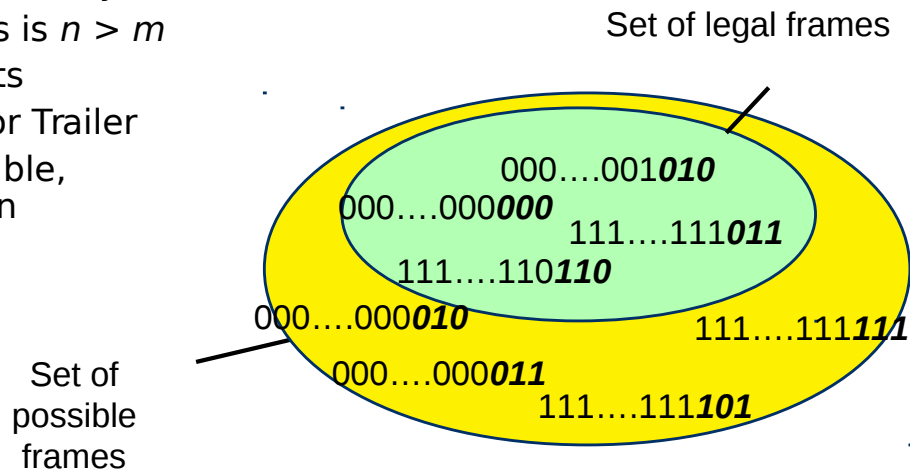
Redundancy

- Redundancy is a precondition of error control
- Without redundancy
 - a frame of length m can represent 2^m possible data,
 - each of them is legal
- A bit error results in new data content



Redundancy

- Main idea:
 - Some possible m -bit sequences are illegal
 - For the representation of 2^m different data,
 - $> 2^m$ possible frames are necessary
 - $> m$ bits are necessary within a frame
 - Length of the frames is $n > m$
 - $r = m - n$ redundant bits
 - Pl. Header and/or Trailer
- Error control is just possible, if we distinguish between legal and illegal frames



Illegal Frames

- The sender only sends legal frames
- In the physical layer bit errors can occur
- Hope:
 - Error in a legal frame always leads to an illegal frame
 - Never to another legal frame
- Necessary condition:
 - The number of bits altered in the physical layer is bounded by a certain number
 - e.g. $\leq k$ bits per frame
- The legal frames are sufficiently different, in order to recognize this frame error rate

Simplest Redundancy: Parity Bit

- A simple rule for adding a redundant bit (i.e., $n=m+1$): is the parity
- **Odd parity**
 - Insert 0, if the number of 1s is odd, otherwise, insert 1
- **Even parity**
 - Insert 0, if the number of 1s is even, otherwise, insert 1
- Example:
 - Original message without redundancy: 01101011001
 - Odd parity: 01101011001**1**
 - Even parity: 01101011001**0**

Error Detection: CRC

Efficient error detection: Cyclic Redundancy Check (CRC)

Often used in practice

High error detection rate

Hardware implementation is easy

Based on polynomial arithmetic over the field Z_2

Bit string is interpreted as representing a polynomial

Coefficients 0 and 1 are possible, interpreted modulo 2

Computing in Z_2

Arithmetic modulo 2:

Rules:

addition mod 2 subtraction mod 2 multiplication mod 2

A	B	A + B
0	0	0
0	1	1
1	0	1
1	1	0

A	B	A - B
0	0	0
0	1	1
1	0	1
1	1	0

A	B	A · B
0	0	0
0	1	0
1	0	0
1	1	1

Example: 0110111011
+ 1101010110
= 1011101101

Polynomial Arithmetic Modulo 2

- Consider polynomials over the field Z_2
 - $p(x) = a_n \cdot x^n + \dots + a_1 x^1 + a_0$
 - Coefficients a_i and variables x are $a_i, x \in \{0,1\}$
 - Computation modulo 2
- Addition, subtraction, multiplication and division (with remainder) of polynomials, as known

Bit Strings and Polynomials of Z_2

- Idea:
 - Consider the bit strings of n bits as coefficients of a polynomial
- Bit string: $b_n b_{n-1} \dots b_1 b_0$
Polynomial: $b_n \cdot x^n + \dots + b_1 \cdot x^1 + b_0$
- A bit string of $(n+1)$ bits corresponds to a polynomial of degree n
- Isomorphism
 - $A \text{ xor } B = A(x) + B(x)$
 - A left shift of A with k position corresponds to:
 - $C(x) = A(x) \cdot x^k$
 - By this isomorphism, we can define division with bit strings

Division by Bit Strings

Example:

$1101010101 : 1001 = 1100110$ remainder 11

1001

1000

1001

001101

1001

1000

1001

0011

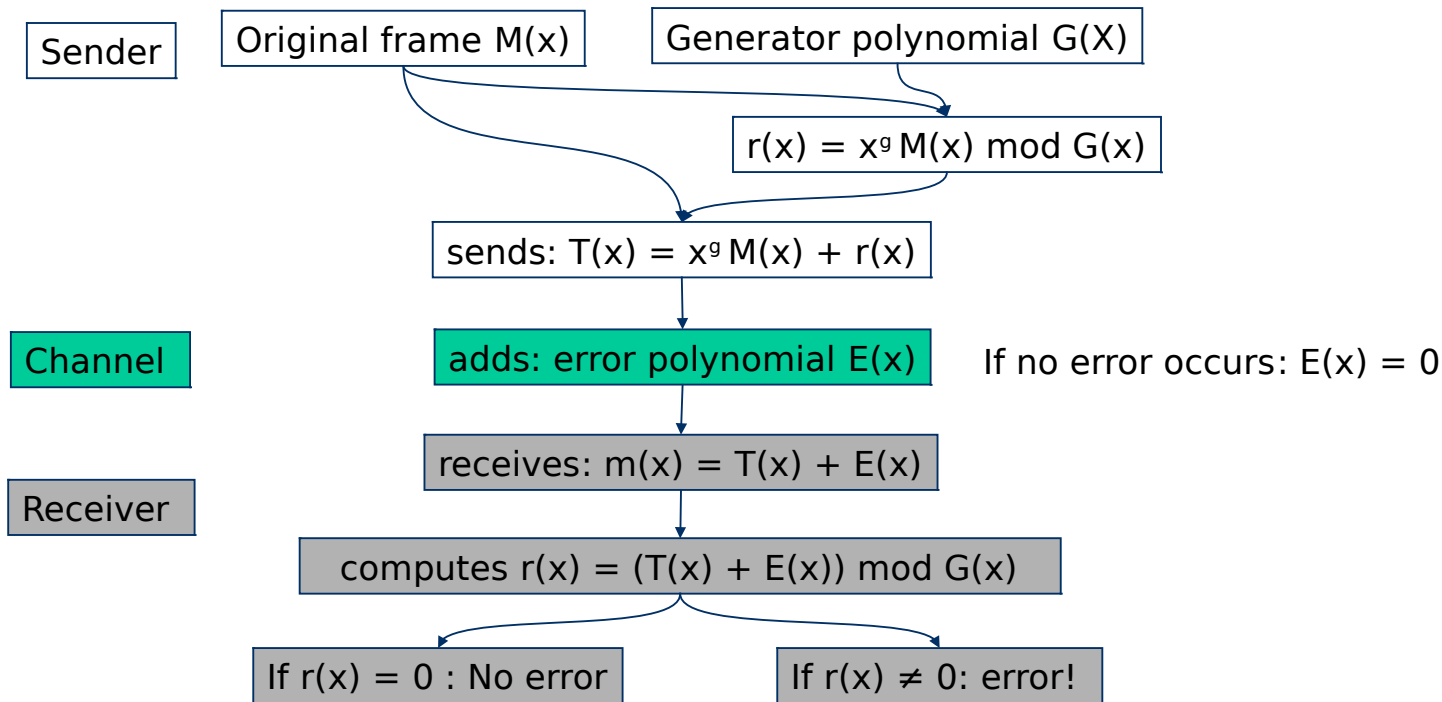
Redundancy by Polynomials: CRC

- Define a generator polynomial $G(x)$ of degree g
 - $G(x)$ is known by sender and receiver
 - we generate g redundant bits
- Given:
 - A frame (message) M , as a polynomial $M(x)$
- Sender
 - Computes the value $r(x) = x^g M(x) \bmod G(x)$
 - Sends: $T(x) = x^g M(x) + r(x)$
 - Note: $x^g M(x) + r(x)$ is a multiple of $G(x)$
- Receiver
 - Receives $m(x)$
 - Computes the remainder: $m(x) \bmod G(x)$

CRC

- If no error occurred:
 - $T(x)$ is received correctly
- Bit error: $T(x)$ contains altered bits
 - This is equivalent to the addition of an error polynomial $E(x)$
 - The receiver receives $m(x) = T(x) + E(x)$
- Receiver
 - Computes the remainder $m(x) \bmod G(x)$
 - If no error: $m(x) = T(x)$,
 - The remainder is 0
 - Bit errors: $m(x) \bmod G(x) = (T(x) + E(x)) \bmod G(x)$
$$= \underbrace{T(x) \bmod G(x)}_0 + \underbrace{E(x) \bmod G(x)}_{\text{error indicator}}$$

CRC – Overview



The Generator Determines the Properties of the CRC

- Bit errors are not recognized if and only if $E(x)$ is a multiple of $G(x)$
- Choosing $G(x)$:
 - 1-bit-error: $E(x) = x^i$ error at position i
 - If $G(x)$ contains at least 2 non-0 coefficients, then $E(x)$ is not a multiple
 - 2-bit-errors: $E(x) = x^i + x^j = x^i (x^{i-j} + 1)$, where $i > j$
 - $G(x)$ must not divide $(x^h + 1)$, for all h , $0 \leq h \leq k$, where k is the maximum frame size
 - Odd number of errors:
 - Then $E(x)$ is not a multiple of $(x+1)$
 - Idea: Let $(x+1)$ be a factor of $G(x)$
 - then $E(x)$ is not a multiple of $G(x)$
- By clever choice of $G(x)$, all burst errors of length $\leq r$ can be detected

CRC in Practice

- The generator polynomial of the IEEE 802.3 (Ethernet) standard (CRC-32):
 - $x^{32} + x^{26} + x^{23} + x^{22} + x^{16} + x^{12} + x^{11} + x^{10} + x^8 + x^7 + x^5 + x^4 + x^2 + x + 1$
- In practice, residual errors after CRC check are ignored
 - But they may still happen! If $E(x)$ is a multiple of $G(x)$.
- Implementation in hardware:
 - Simple XOR operation
 - HW implementation: shift register circuit
 - Negligible overhead in hardware

Literature

- Andrew S. Tanenbaum and David J. Wetherall: Computer Networks. Pearson, 5 edition, 2010.